

2M2H 3.4 Factoring Differences of Squares ANSWERS

1. How can you tell whether a binomial is a difference of squares?

Both terms are perfect squares and they are being subtracted.

2. How can you tell if a trinomial is a perfect square trinomial?

- 3 terms
- 1st and 3rd terms are perfect squares
- Middle term is double the square root of the 1st and 3rd terms

Factor each binomial completely, if possible. Don't forget to check for common factors.

3. $x^2 - 1$

$(x + 1)(x - 1)$

4. $36m^2 - 49$

$(6m + 7)(6m - 7)$

5. $q^2 + 49$

prime

6. $16x^2 + 25$

prime

7. $81v^2 - 225y^2$

$9(3v + 5y)(3v - 5y)$

8. $x^4 - 9$

$(x^2 + 3)(x^2 - 3)$

Determine if the following are perfect square trinomials. If they are perfect square trinomials, factor them using the identity.

9. $x^2 + 8x + 16$

$(x + 4)(x + 4)$

10. $x^2 - 10x + 25$

$(x - 5)(x - 5)$

11. $x^2 + 14x - 49$

Not Perfect Square Trinomial
Subtract in front of 49

12. $x^2 - x + 20$

Not Perfect Square Trinomial
20 is not a perfect square

13. $9x^2 + 24x + 25$

Not Perfect Square Trinomial
Middle Term is not
double square root of 1st and 3rd terms

14. $25x^2 + 90x + 81$

$(5x + 9)(5x + 9)$

Factor each polynomial completely. Don't forget to check for a common factor first. If the polynomial is prime, say so.

15. $y^2 - 121$

$$(y + 11)(y - 11)$$

16. $2v^2 - 32$

$$2(v + 4)(v - 4)$$

17. $w^2 + w - 6$

$$(w - 2)(w + 3)$$

18. $-8v + 12$

$$-4(2v - 3)$$

19. $6x^2 - 13x + 5$

$$(2x - 1)(3x - 5)$$

20. $-3k^2 - 24k + 60$

$$-3(k + 10)(k - 2)$$

21. $144 - 49t^2$

$$(12 + 7t)(12 - 7t)$$

22. $3x^2 + 75$

$$3(x^2 + 25)$$

23. $3x^2 + 5x - 28$

$$(3x - 7)(x + 4)$$

24. $v^2 - 8v + 12$

$$(v - 2)(v - 6)$$

25. $4x^2 + 19x - 30$

$$(4x - 5)(x + 6)$$

26. $2t^2 - 5t + 3$

$$(2t - 3)(t - 1)$$

27. $25a^2 - 121b^2$

$$(5a + 11b)(5a - 11b)$$

28. $-18p^2 + 32q^2$

$$-2(3p + 4q)(3p - 4q)$$

29. $x^4 - 81$

$$(x^2 + 9)(x + 3)(x - 3)$$

Solve each equation.

30. $\frac{x - 8}{2x + 5} = 4$

$$x = -4$$

31. $-(x - 16) - x = -5x$

$$x = -\frac{16}{3}$$