SM 2

Date:

Section: 1.1

Objective: Functions

Function: When each domain element is paired with a unique range element.

- Only 1 y-value for every x-value
- For every input there is one and only one output.

Domain: The set of all inputs (the x-values) of a relation.

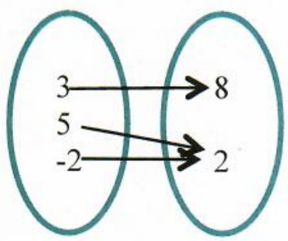
- If a relation is represented by a graph or ordered pairs, the domain is the set of all x-coordinates of points on the graph.

Range: The set of all outputs (the y-values) of a relation.

- If a relation is represented by a graph or ordered pairs, the range is the set of all y-coordinates of points on the graph.

Examples: Decide whether each relation is a function. Then write the relation as a set of ordered pairs. Then find the domain and range.

1.



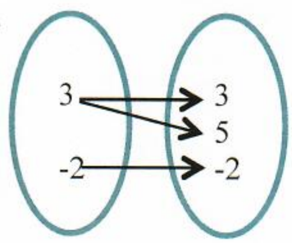
Function:

Ordered Pairs:

Domain:

Range:

2.



Function:

Ordered Pairs:

Domain:

Range:

3.

x	y
-2	5
-1	7
0	9
1	-2
2	-2

Function:

Domain:

Range:

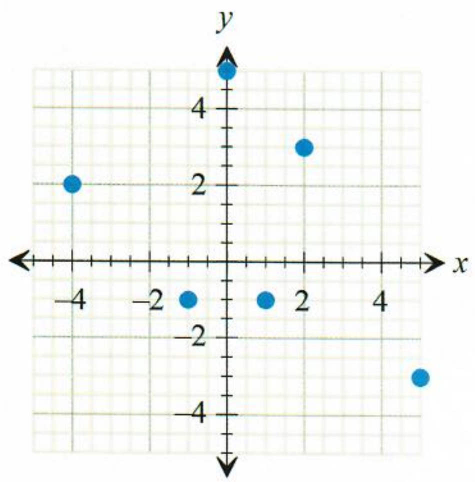
4. $\{(4,-7),(-1,5),(8,2),(4,5)\}$

Function:

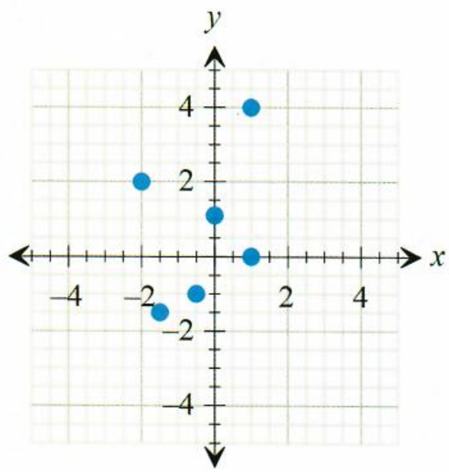
Domain:

Range:

5.



6.



Function:

Ordered Pairs:

Domain:

Range:

Function:

Ordered Pairs:

Domain:

Range:

Domain and Range in Real Life Situations: In real life situations, it's important to think through what values make sense in the problem. You also need to think about what x stands for and what y stands for.

Examples: Determine if the situation is a function. Describe the domain and range for each real world situation.

a) A teacher creates a list of ice cream flavors on the board. Then she has each student write their name next to the ice cream flavor they like best of the ones listed.

Is this a function? Why or why not?

Domain:

Range:

b) A teacher creates a table with the student's name in the first column. Then she has the students write down their favorite ice cream flavor next to their name.

Is this a function? Why or why not?

Domain:

Range:

Examples: Describe the domain and range for each real world situation.

c) Your cell phone plan charges a flat fee of $10 for up to 1000 texts and $0.10 per text over 1000. What are the domain and range?

Circle which unit represents the domain: **Money or Texts**

Domain:

Range:

d) You are getting ready for the Homecoming dance. Your dad is going to let you borrow his new car, but you need to wash and fill it. The car wash costs $5 and the gas costs $3.89 per gallon. The car can hold 15 gallons of gas. What are the domain and range if the total cost is a function of the number of gallons and the car is completely empty when you pull into the gas station?

Circle which unit represents the domain: **Money or Gallons**

Domain:

Range:

SM 2

Date: **Section: 1.2 Starter Notes**

Objective: Interval Notation

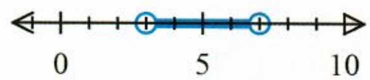
Interval Notation

Domain and range are often written in ***interval notation.***

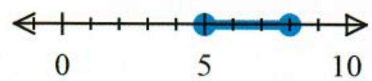
- The numbers are where the interval starts and stops.
- If an endpoint is *included*, put it in a bracket [or]
- If an endpoint is *not included*, put it in parentheses (or)
- If the interval goes on forever, use $-\infty$ or ∞. These always get put in parentheses (or).

Examples:

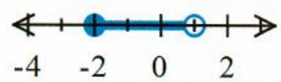
- (3, 7) means everything between 3 and 7, not including either 3 or 7.



- [5, 8] means everything between 5 and 8, including both 5 and 8.

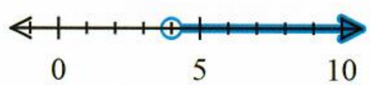


- [–2, 1) means everything between –2 and 1, including –2, but not including 1.

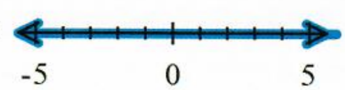


- ($-\infty$, –3] means everything less than or equal to –3.

- (4, ∞) means everything greater than 4.



- ($-\infty$, ∞) means all real numbers (goes on forever in both directions).



Tips

- Use parentheses (or) around numbers that *are not included* in the domain or range.
  - This happens when there is an ***open circle*** at a point or an ***asymptote*** (a line that the graph gets really close to, but never actually touches).
- Use brackets [or] around endpoints that *are included* in the domain or range.
  - It there is a point on the graph with the given *x*- or *y*-coordinate, use a bracket.
- Always use parentheses around $-\infty$ and ∞.
- ***Read the domain from left to right and the range from down to up.***
  - Write the lower value or $-\infty$ first and the higher value or ∞ last.

SM 2

Date: **Section: 1.2**

Objective: Domain and Range

Domain: The set of all inputs (the *x*-values) of a relation.

- If a relation is represented by a graph, the domain is the set of all *x*-coordinates of points on the graph.
- When modeling a real-life situation, the domain is the set of *x*'s that make sense in the problem.
- When given an equation, the domain is the set of x-values for which the equation is defined.

Range: The set of all outputs (the *y*-values) of a relation.

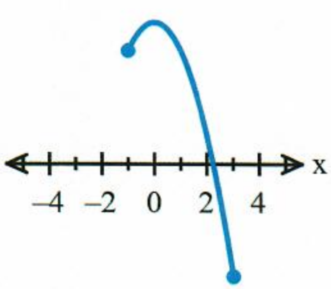
- If a relation is represented by a graph, the range is the set of all *y*-coordinates of points on the graph.
- When modeling a real-life situation, the range is the set of *y*'s that make sense in the problem.

Domain - given the equation of a function. When given an equation, think about what x-values will "work" as input into the equation. Are there any values of x for which the equation is not defined?

Asymptote: A line that the graph approaches but never reaches. It is represented as a dotted line. If the graph has an asymptote, use a parenthesis in your interval notation for domain and range.

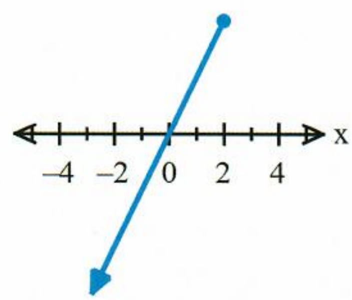
Example: State the domain in interval notation.

a)



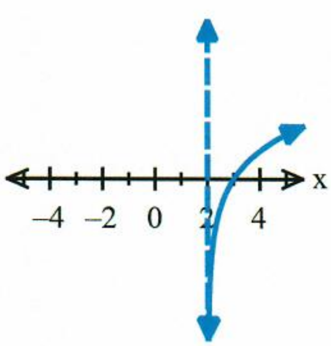
Domain:

b)



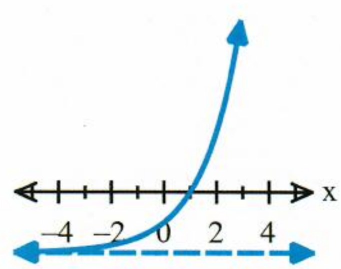
Domain:

c)



Domain:

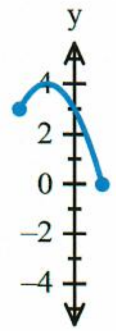
d)



Domain:

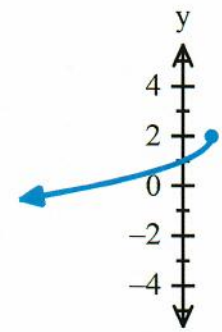
Example: State the range in interval notation.

a)



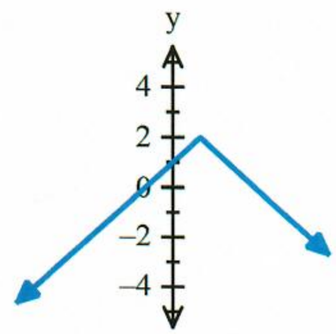
Range:

b)



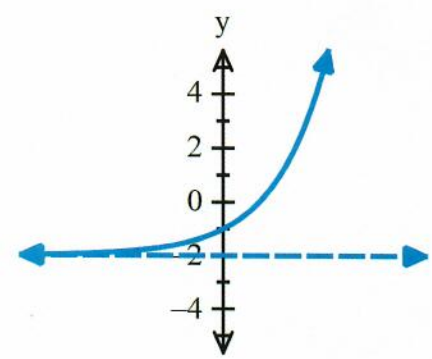
Range:

c)



Range:

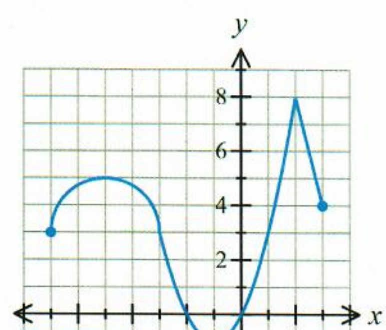
d)



Range:

Examples: Determine whether each graph represents a function. Then state the domain and range given the graph of the function. Write answers in interval notation.

a)

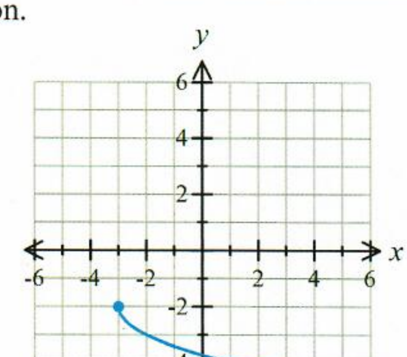


Function?

Domain:

Range:

b)

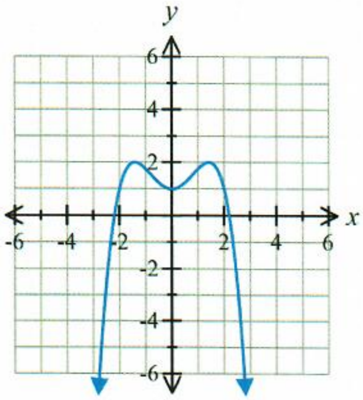


Function?

Domain:

Range:

c)

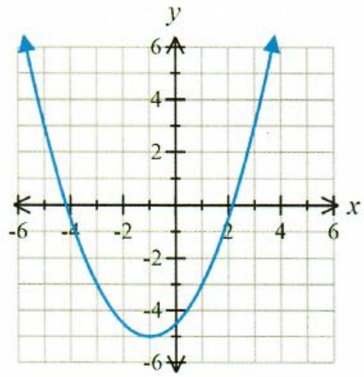


Function?

Domain:

Range:

d)

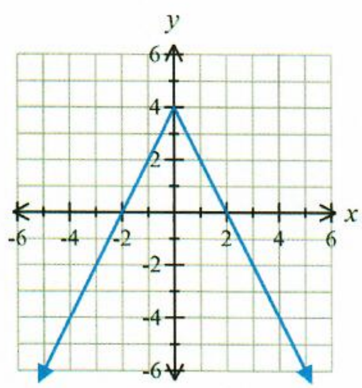


Function?

Domain:

Range:

e)

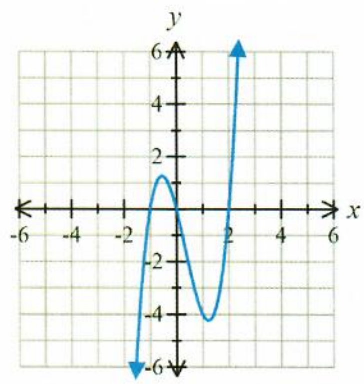


Function?

Domain:

Range:

f)

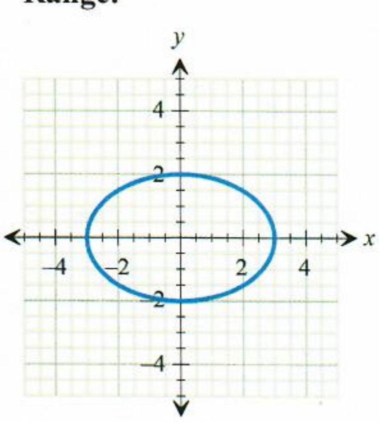


Function?

Domain:

Range:

g)



Function?

Domain:

Range:

SM 2

Date: **Section: 1.3**

Objective: Function Notation

Function notation: Function notation is the way a function is written. $f(x)$ is read "f of x".
x = input
$f(x)$ = output
$f(x)$ is the same as y.

Examples: The graph of $y = f(x)$ is shown below. Use it to answer the following questions.

a) Find $f(-4)$.

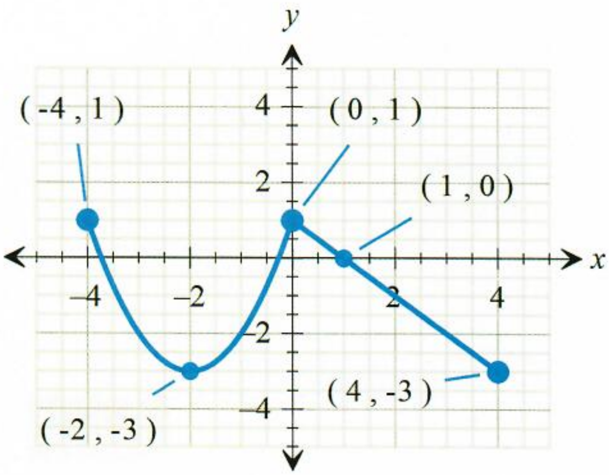
b) Find $f(0)$.

c) For what values of x is $f(x) = 0$?

d) For what values of x is $f(x) = -3$?

e) What is the domain?

f) What is the range?



REVIEW order of operations

a) -4^2

b) $(-4)^2$

c) $-(1+3)^2$

d) $-2(3^2)$

e) $-3 \cdot (-2)^2 + 4$

f) $2|3-5|$

g) $8 + |10-6|$

h) $\frac{2+6}{-4}$

i) $\frac{8}{2(5)+6}$

Evaluating a function or finding a value means substituting the given value for x in the equation. Evaluate the expression. You may use a calculator to evaluate the expression.

Examples: Find each value if $f(x) = x^2 - 2x + 3$, $g(x) = 3x - 5$, **and** $h(x) = \frac{x}{4 - 2x}$.

Leave your answers as simplified fractions, if necessary. Show all your work.

a) $f(2)$

b) $g(-1)$

c) $h(4)$

d) $g\left(\frac{2}{3}\right)$

e) $f(-5)$

f) $h(-3)$

SM 2

Date:

Section: 1.4

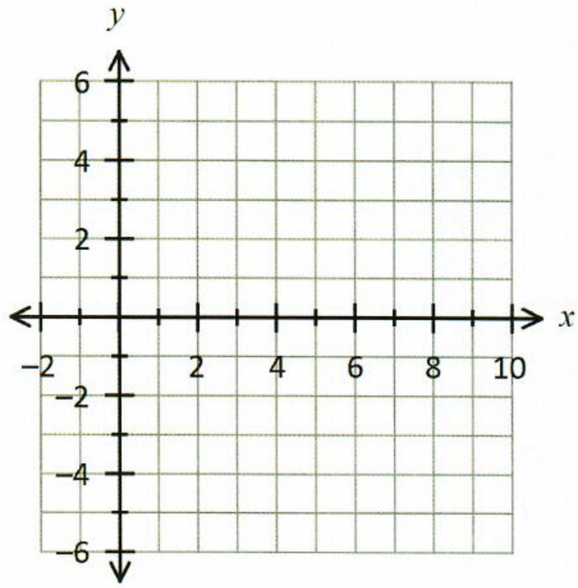
Objective: Parent Graphs and Transformations

Parent Graphs - Fill in the table to find some **key points** for some important graphs. Use the table to generate ordered pairs for points on the graph, then sketch the graph.

★ **Square Root Function:** $f(x) = \sqrt{x}$

Domain:_______________ Range:_______________

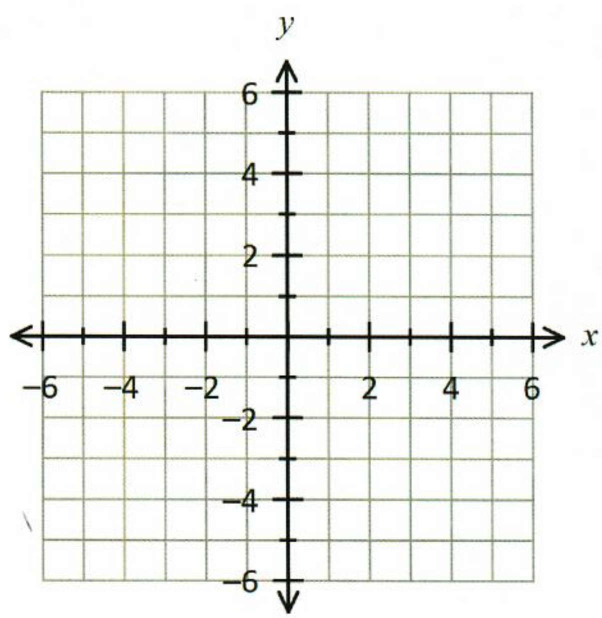
x	work	y	point
–1			
0			
1			
4			
9			



★ **Absolute Value Function:** $f(x) = |x|$

Domain:_______________ Range:_______________

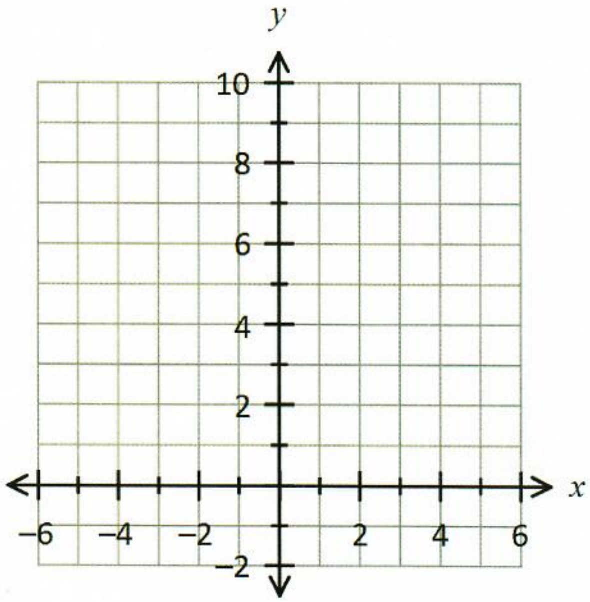
x	work	y	point
–2			
–1			
0			
1			
2			



★ **Quadratic Function:** $f(x) = x^2$

Domain:_______________ Range:_______________

x	work	y	*point*
−2			
−1			
0			
1			
2			



Types of transformations

Transformations, like arithmetic operations, need to be applied in a particular order. Here is the correct "Order of Transformations."

1. **Reflection**:
   a. Vertical Reflection – graph is reflected over the x-axis
   b. Horizontal Reflection – graph is reflected over the y-axis
2. **Stretch/Compression:**
   We will restrict our attention to Vertical stretches/compressions.
   a. Vertical Stretch – the y-coordinates are multiplied by a scalar that is greater than 1
   b. Vertical Compression – the y-coordinates are multiplied by a scalar that is between 0 and 1
3. **Translation (or Shift)**:
   a. Horizontal Translation – graph is shifted to the left or right
   b. Vertical Translation – graph is shifted up or down

Transformations of the parent graph:

	$f(x)=\lvert x\rvert$	$f(x)=x^2$	$f(x)=\sqrt{x}$	Effect on Parent Graph
$y=-f(x)$				
$y=2f(x)$				
$y=\frac{1}{2}f(x)$				
$y=f(x)+2$				
$y=f(x)-2$				
$y=f(x+2)$				
$y=f(x-2)$				

SM 2

Date: Section: 1.5

Objective: One-Step Transformations

A. Types of transformations

Transformations, like arithmetic operations, need to be applied in a particular order. Here is the correct "Order of Transformations."

1. **Reflection**:
   a. Vertical Reflection – graph is reflected over the x-axis
   b. Horizontal Reflection – graph is reflected over the y-axis
2. **Stretch/Compression (Dilation)**:
   We will restrict our attention to Vertical stretches/compressions.
   a. Vertical Stretch (dilate by a factor) – the y-coordinates are multiplied by a scalar that is greater than 1
   b. Vertical Compression (dilate by a factor) – the y-coordinates are multiplied by a scalar that is between 0 and 1
3. **Translation (or Shift)**:
   a. Horizontal Translation – graph is shifted to the left or right
   b. Vertical Translation – graph is shifted up or down

B. Applying Transformations to the Function:

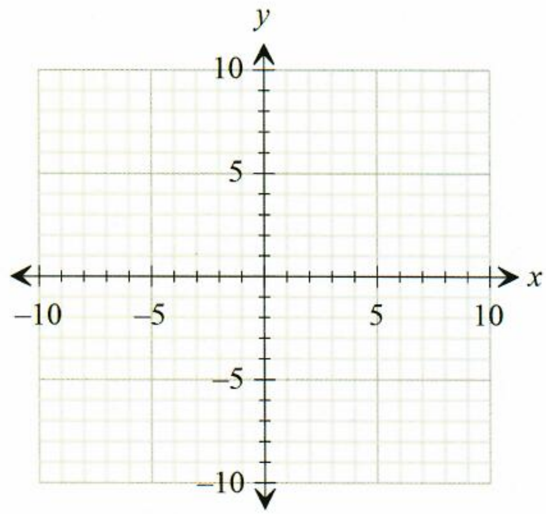
For each graph, do the following:

1. **Identify the parent graph ($y = |x|$, $y = x^2$, or $y = \sqrt{x}$).**
2. **Fill in the *x*, *y* table for the parent graph.**
3. **Draw the graph of the parent graph with a dashed line.**
4. **Identify the transformation.**
5. **Fill in the *x*, *y* table for the transformation.**
6. **Draw the final graph with a solid line.**

Vertical reflection/Reflection over the x-axis:

1. $f(x) = -\sqrt{x}$

	x	$y = \sqrt{x}$			
	0				
	1				
	4				
	9				



Parent Graph:

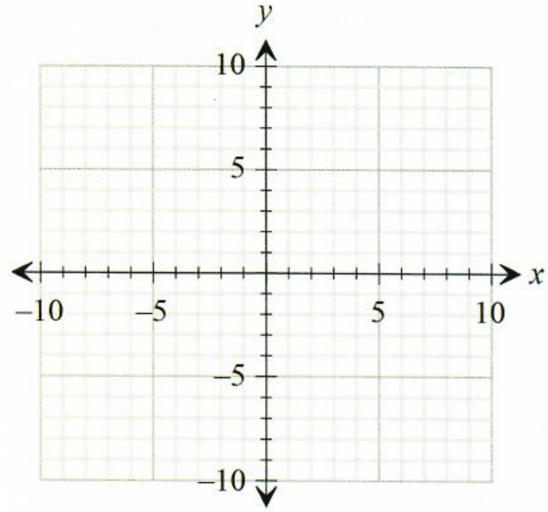
Transformation:

2. $f(x) = -|x|$

	x	$y = \|x\|$			
	-2				
	-1				
	0				
	1				
	2				

Parent Graph:

Transformation:



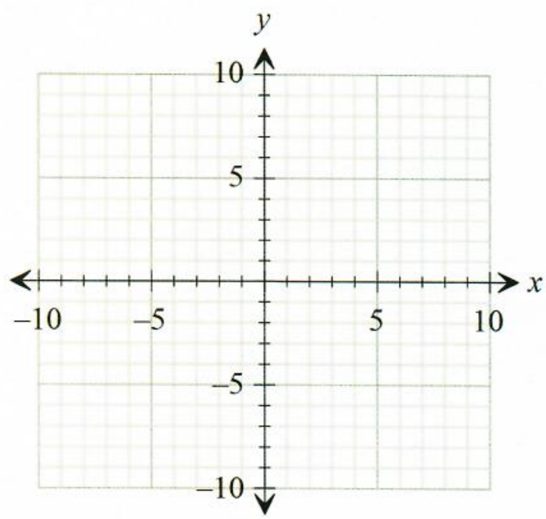
Vertical stretch/compression:

3. $f(x) = 2\sqrt{x}$

	x	$y = \sqrt{x}$			
	0				
	1				
	4				
	9				

Parent Graph:

Transformation:

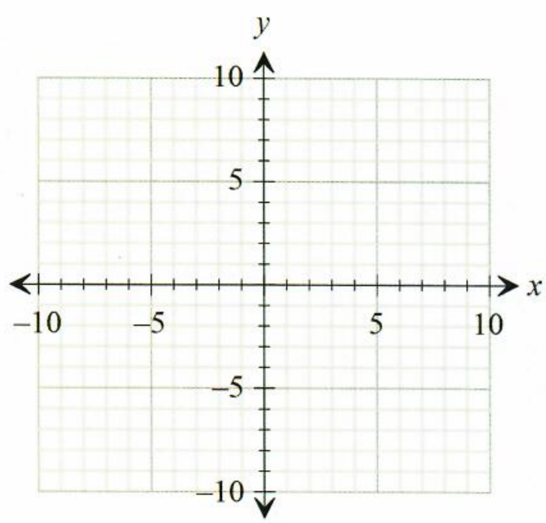


4. $f(x) = \frac{1}{2}x^2$

	x	$y = x^2$			
	-2				
	-1				
	0				
	1				
	2				

Parent Graph:

Transformation:

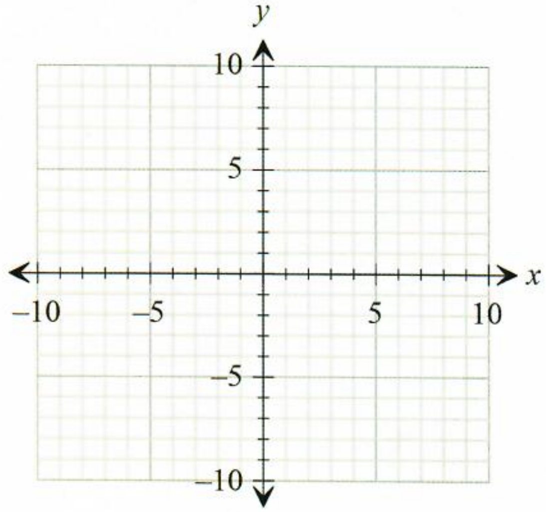


Horizontal Translation:

★ **ALWAYS do the opposite of the horizontal number.**

5. $f(x) = \sqrt{x-3}$

	x	$y=\sqrt{x}$			
	0				
	1				
	4				
	9				

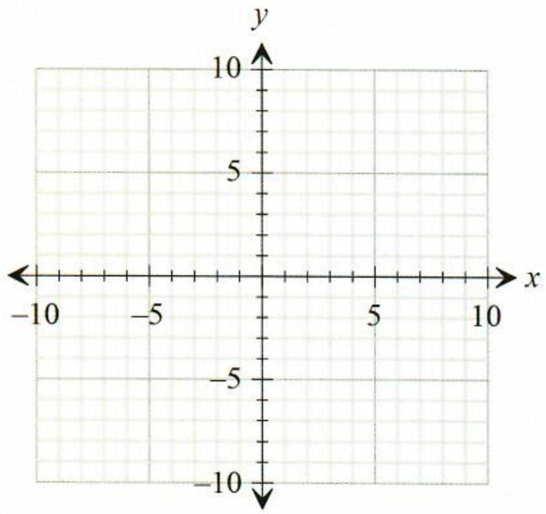


Parent Graph:

Transformation:

6. $f(x) = |x+4|$

	x	$y=\lvert x\rvert$			
	-2				
	-1				
	0				
	1				
	2				



Parent Graph:

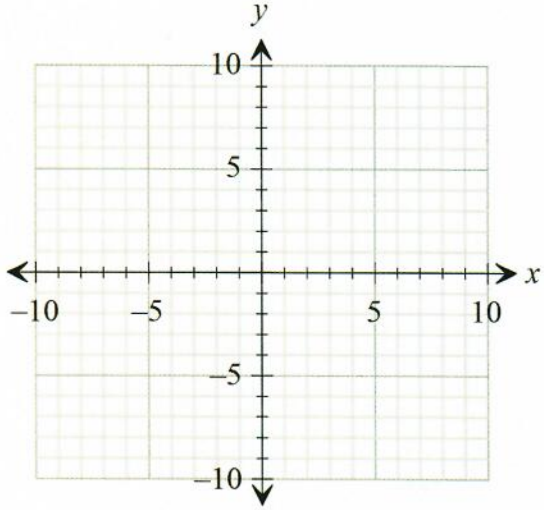
Transformation:

This is what a horizontal translation looks in a quadratic function. $f(x) = (x+4)^2$

Vertical Translation:

7. $f(x) = |x| + 3$

	x	$y = \|x\|$			
	-2				
	-1				
	0				
	1				
	2				

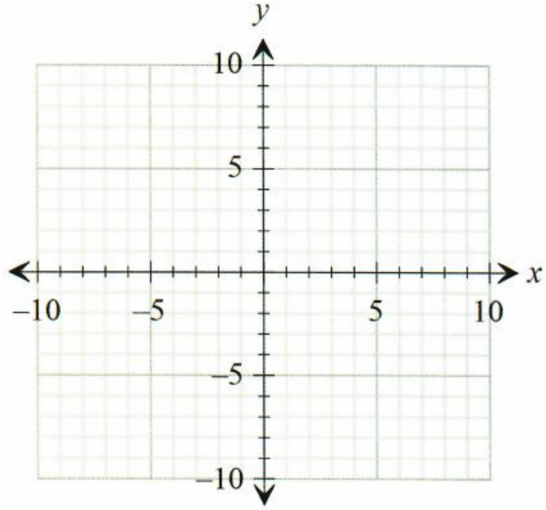


Parent Graph:

Transformation:

8. $f(x) = x^2 - 2$

	x	$y = x^2$			
	-2				
	-1				
	0				
	1				
	2				



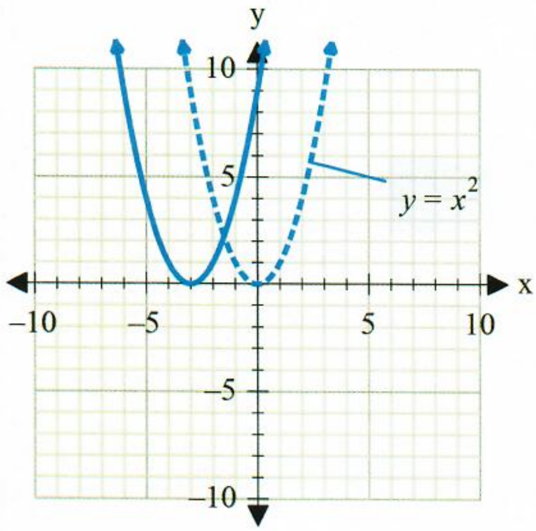
Parent Graph:

Transformation:

C. **Given the graph, write the equation of the function.**

On each graph, the parent graph is shown as a dashed line, and a transformed graph is shown as a solid line. Determine what transformation of the parent graph was performed and write an equation of the final graph.

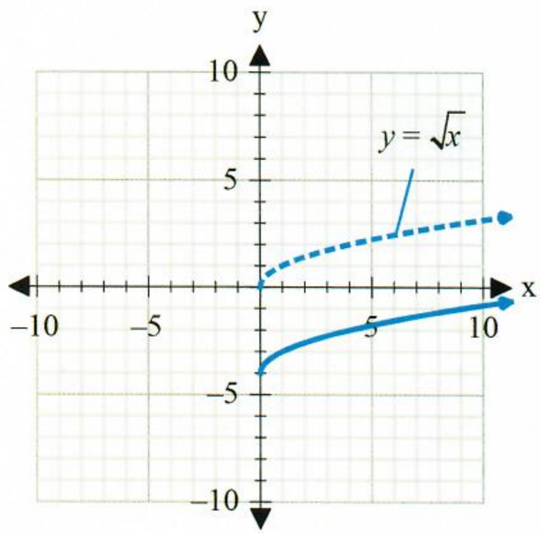
9.



Transformation:________________________

Equation:___________________________

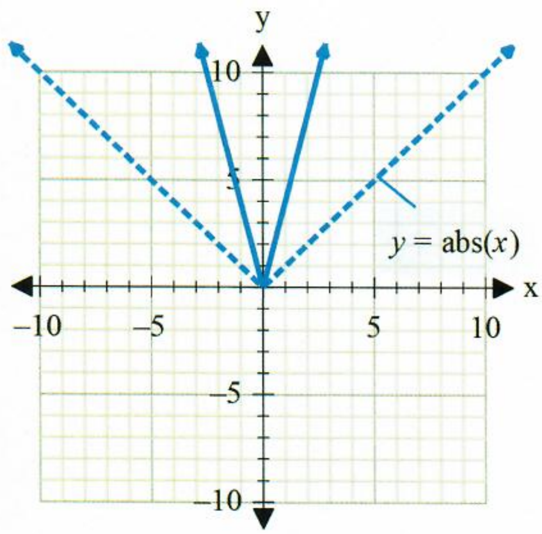
10.



Transformation:________________________

Equation:___________________________

11.



Transformation:________________________

Equation:___________________________

SM 2

Date: Section: 1.6

Objective: Multiple-Step Transformations

A. Types of transformations

Transformations, like arithmetic operations, need to be applied in a particular order. Here is the correct **"Order of Transformations."**

1. **Reflection (the negative in front of the equation)**:
   a. Vertical Reflection – graph is reflected over the x-axis
   b. Horizontal Reflection – graph is reflected over the y-axis
2. **Stretch/Compression (the number in front of the equation or a):**
   We will restrict our attention to Vertical stretches/compressions.
   a. Vertical Stretch – the y-coordinates are multiplied by a scalar that is greater than 1
   b. Vertical Compression – the y-coordinates are multiplied by a scalar that is between 0 and 1
3. **Translation (or Shift)**:
   a. Horizontal Translation – graph is shifted to the left or right (the opposite of the number with x, or in the parentheses with x, or h)
   b. Vertical Translation – graph is shifted up or down (the number that is added or subtracted to the equation or k)

B. Finding the number that tells you the transformation

Answer the following questions using the equations: $y = a\sqrt{(x-h)} + k$, $y = a((x-h))^2 + k$, $y = a|(x-h)| + k$. Given the following equations find a, h, and k.

A. $y = 3\sqrt{x-6} + 8$

a=__________________

h=__________________

k=__________________

B. $y = (x-4)^2 - 2$

a=__________________

h=__________________

k=__________________

C. $y = -2|x| + 7$

a=__________________

h=__________________

k=__________________

C. Writing transformations in the correct order

For each function, identify the parent graph ($y = \sqrt{x}$, $y = x^2$, or $y = |x|$), then list the transformations needed to get from the parent graph to the final graph. Make sure to list the transformations in the order in which they should be applied.

A. $y = -4(x+2)^2$

Parent: ____________

Transformations:

1.

2.

3.

B. $y = \frac{1}{4}|x+3| - 6$

Parent: ____________

Transformations:

1.

2.

3.

C. $y = -2\sqrt{x} - 1$

Parent: ____________

Transformations:

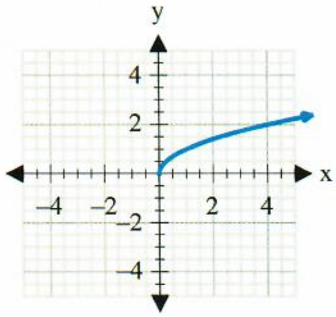
1.

2.

3.

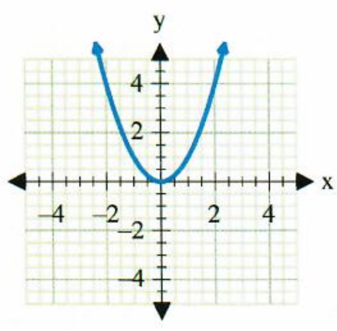
D. Vocabulary

a. Endpoint:

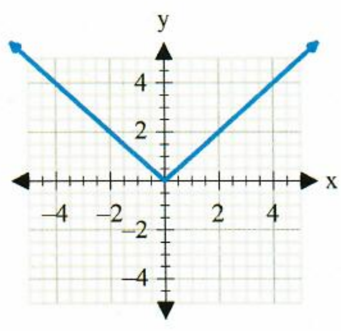


Endpoint:___________

b. Vertex:



Vertex: _____________



Vertex: _____________

E. How to put a, h, and k in the table

A. $y = 2(x-3)^2 + 1$

a=____________________ h=____________________ k=____________________

Parent Columns:

Column for stretch and reflection: **Multiply the y-value of the Parent columns by a**

Column for translation or shift: **Add h to x-value of the previous column** **Add k to y-value of the previous column**

	x	$y = x^2$			
	-2				
	-1				
	0				
	1				
	2				

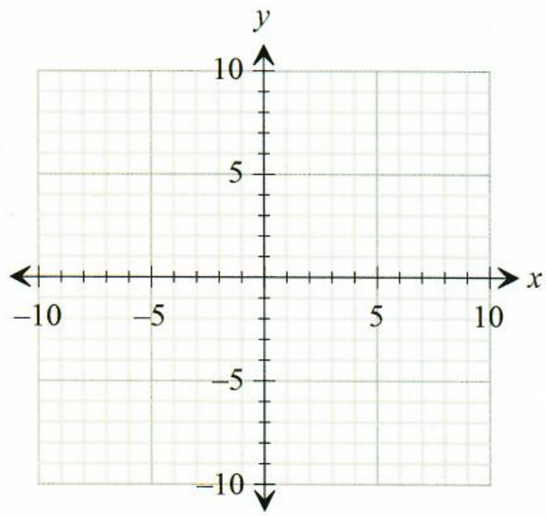
F. Graphing multiple-step transformations:

For each graph, do the following:

1. **Identify the parent graph ($y = |x|$, $y = x^2$, or $y = \sqrt{x}$).**
2. **Fill in the x, y table for the parent graph.**
3. **Draw the graph of the parent graph with a dashed line.**
4. **List the transformations in the correct order.**
5. **Fill in the table to apply the reflections and stretches/compressions (by multiplying the y-coordinates by the number in front or multiply by a).**
6. **Fill in the table to apply the translations. (Add or subtract h and k from the x's and y's to move the graph in the correct directions.)**
7. **Draw the final graph with a solid line.**
8. **State the vertex or endpoint, domain, and range of the final graph.**

A. $f(x) = -x^2 - 2$ a=______________ h=______________ k=______________

	x	$y = x^2$			
	-2				
	-1				
	0				
	1				
	2				



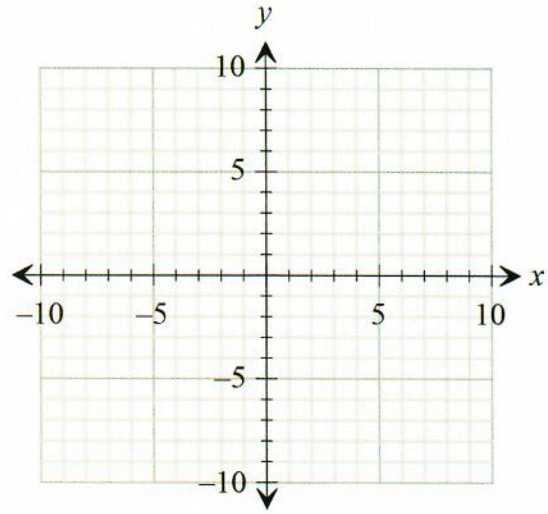
Parent Graph:______________

Transformations:

Vertex:______________ Domain:______________ Range:______________

B. $f(x) = \frac{1}{2}|x+1| - 3$ a=______________ h=______________ k=______________

	x	$y=\|x\|$			
	-2				
	-1				
	0				
	1				
	2				



Parent Graph:______________

Transformations:

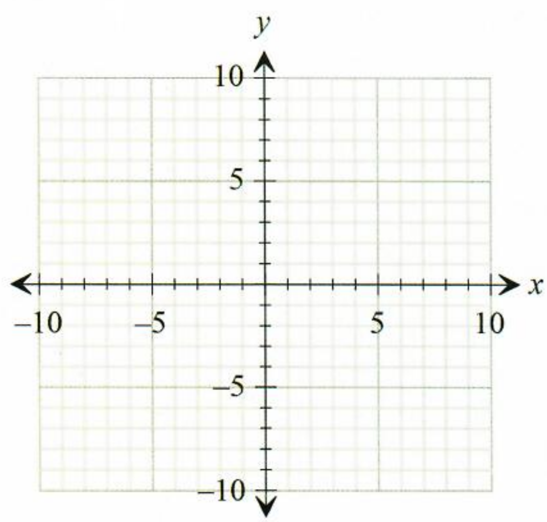
Vertex:______________

Domain:______________

Range:______________

C. $f(x) = \frac{1}{2}\sqrt{x+1} - 3$ a=______________ h=______________ k=______________

	x	$y=\sqrt{x}$			
	0				
	1				
	4				
	9				



Parent Graph:______________

Transformations:

Vertex:______________

Domain:______________

Range:______________

Write an equation for each translation of the **parent function $y = \sqrt{x}$.**

A: 5 unit up: ________________

a=______________ h=_____________ k=_____________

B: 8 units to the right: ______________

a=______________ h=_____________ k=_____________

Write an equation for each translation of the **parent function $y = x^2$.**

C: 5 units left, 12 units down: __________________

a=______________ h=_____________ k=_____________

D: Vertical stretch by a factor of $\frac{1}{2}$, 9 units right: ___________________

a=______________ h=_____________ k=_____________

Write an equation for each translation of the **parent function $y = |x|$**

E: Vertical stretch by a factor of 4, reflect over the x-axis, 10 units up: ________________________

a=______________ h=_____________ k=_____________